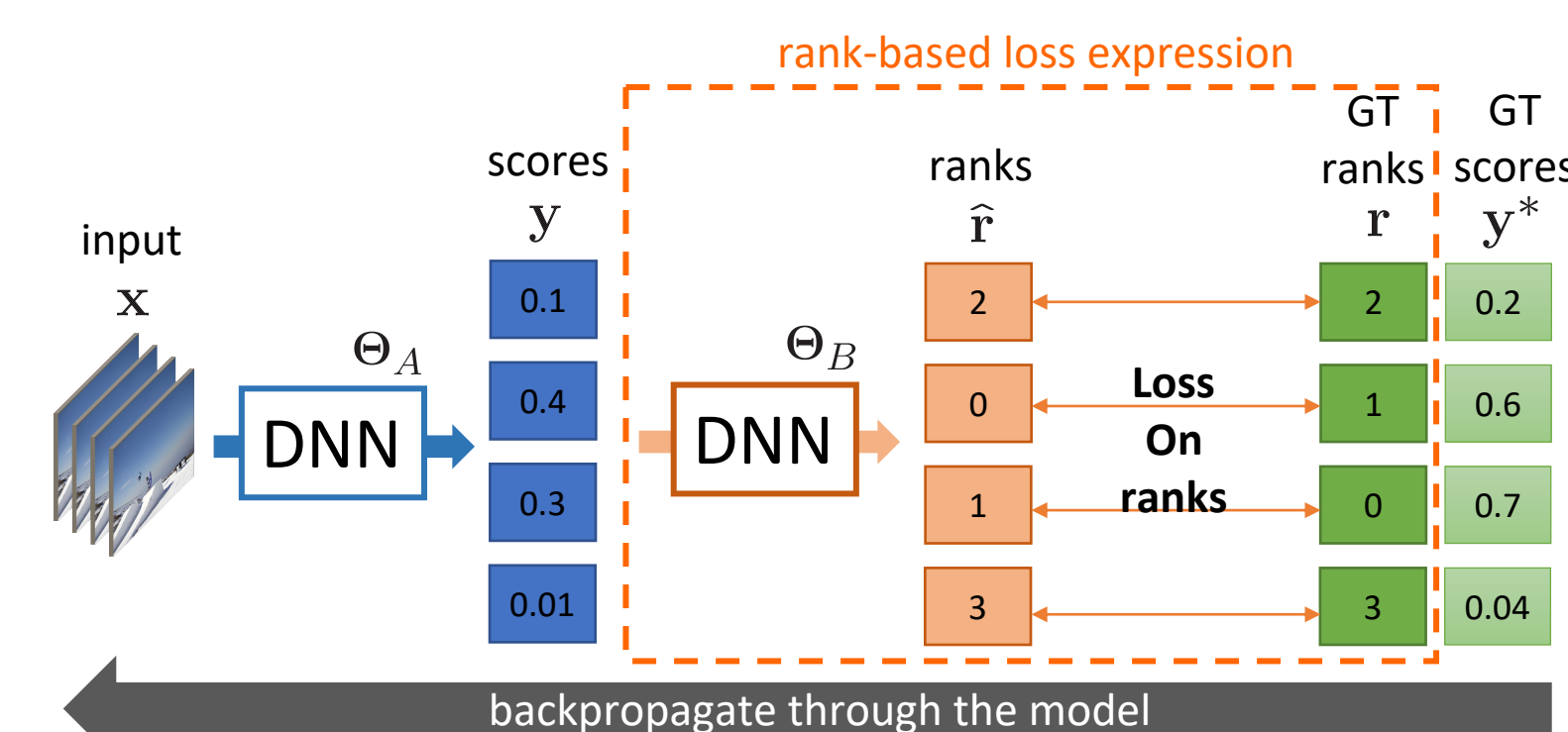


Overview

Non-differentiable ranking metrics:

The projection from continuous score to discrete rank used in ranking metrics makes them non-differentiable



Approach to make ranking metrics differentiable:

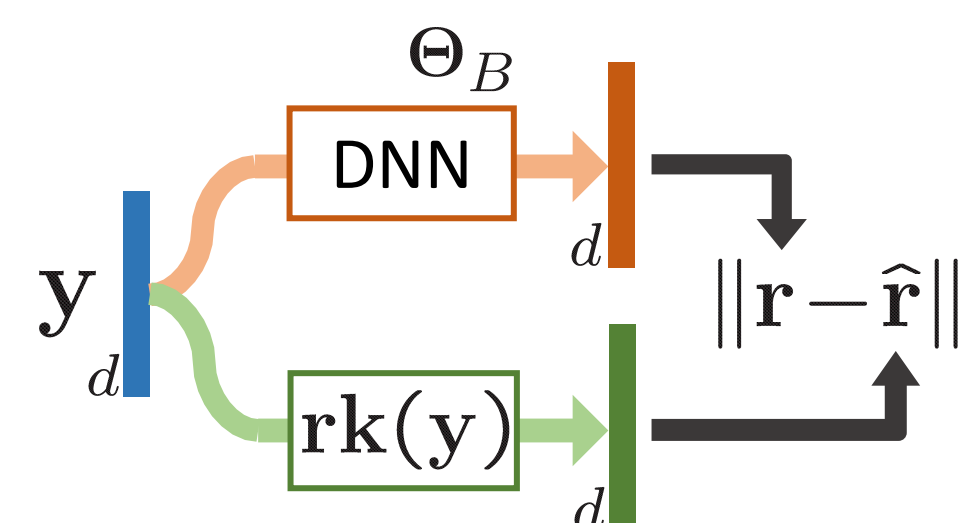
- DNN sorter trained to approximate the rank function rk
- Ranking metrics expressed as a function of the sorter
- Ranking metrics used as loss function

Training a differentiable sorter

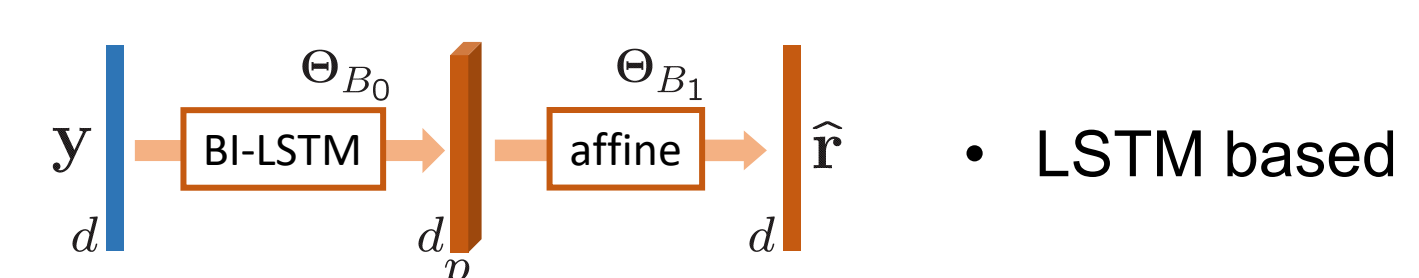
Using only synthetic data:

- Uniform distribution over $[-1, 1]$
- Normal distribution with $\mu = 0$ and $\sigma = 1$
- Evenly spaced numbers in random sub-range of $[-1, 1]$

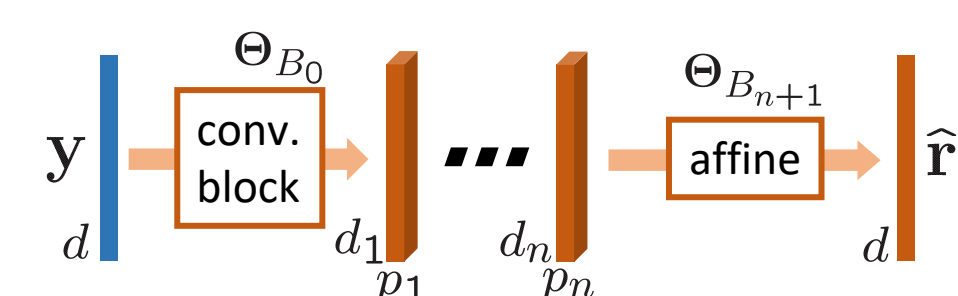
Training:



Sorter architecture:



- Convolution based



Loss functions

Spearman correlation as loss function:

- Spearman correlation

$$r_s = 1 - \frac{6\|\text{rk}(\mathbf{y}) - \text{rk}(\mathbf{y}')\|_2^2}{d(d^2 - 1)}$$

- Maximizing Spearman correlation

$$\min_{\Theta_A} \sum_{n=1}^N \|\text{rk}(\mathbf{y}^{(n)}) - \text{rk}(\mathbf{y}^{*(n)})\|_2^2$$

- Replacing rk with our trained sorter

$$\mathcal{L}_{SPR}(\Theta_A, \mathcal{B}) = \sum_{n=1}^N \left\| f_{\Theta_B}(\mathbf{y}(\Theta_A)^{(n)}) - \text{rk}(\mathbf{y}^{*(n)}) \right\|_2^2$$

Mean average precision as loss function:

$$\mathcal{L}_{mAP}(\Theta_A, \mathcal{B}) = \sum_{c=1}^C \langle f_{\Theta_B}(\mathbf{y}_c), \mathbf{y}_c^* \rangle$$

Recall as loss function:

$$\mathcal{L}_{REC}(\Theta_A, \mathcal{B}) = \frac{1}{d} \sum_{i \in \mathcal{B}} \max_{c \neq p, c \neq i} \text{loss}(\mathbf{Y}[i], p, c)$$

$$\text{loss}(\mathbf{Y}[i], p, c) = \max \{0, \alpha + f_{\Theta_B}(\mathbf{Y}[i])_p - f_{\Theta_B}(\mathbf{Y}[i])_c\}$$

Handcrafted sorter

Baseline: a ranking algorithm

- A differentiable comparator: the sigmoid function

$$\sigma_{comp}(a, b) = \frac{1}{1 + e^{-\lambda(b-a)}}$$

- Comparing an element with the rest of the sequence yields its rank

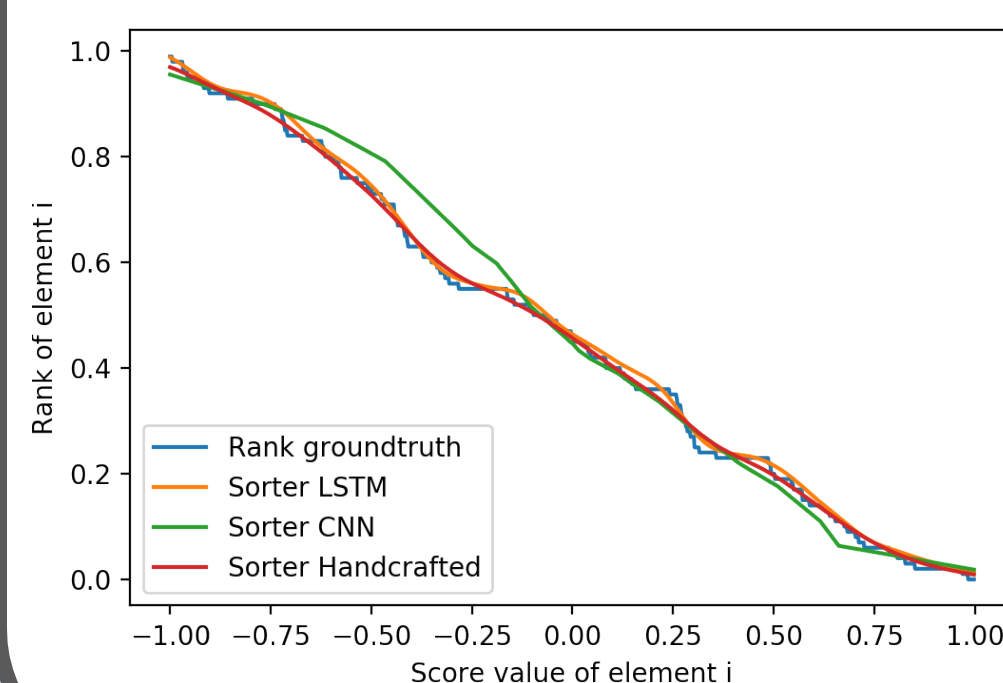
$$f_h(\mathbf{y}, i) = \sum_{j:j \neq i} \sigma_{comp}(\mathbf{y}_i, \mathbf{y}_j)$$

- Value of λ , a trade off between accuracy and gradient flow

Sorter comparison

Sorter behavior analysis:

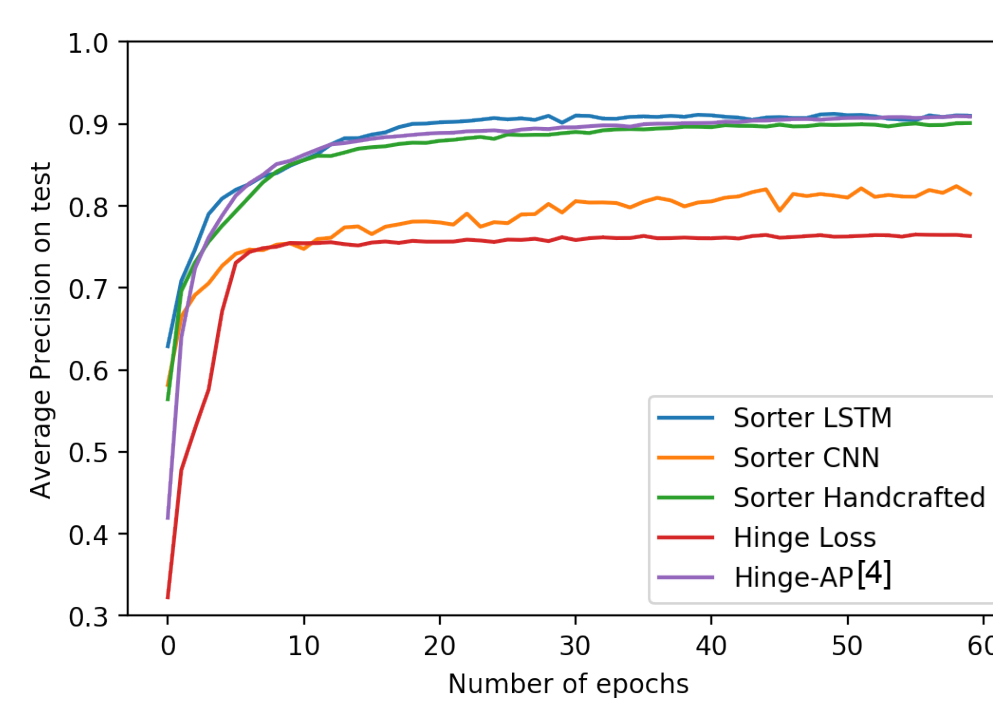
- The learned sorters are able to estimate the groundtruth rank
- RNN sorters perform better than CNN ones



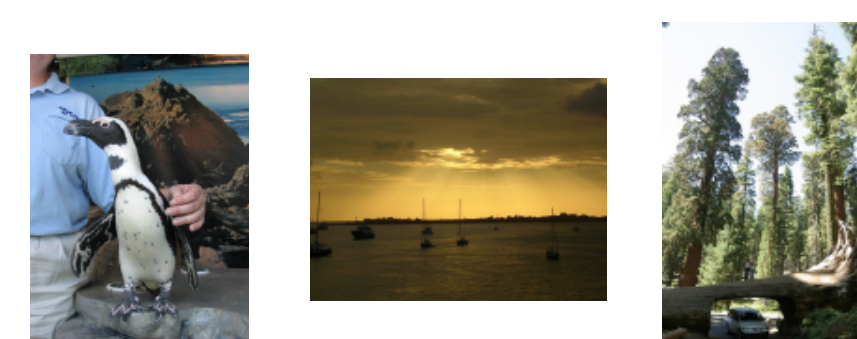
Memorability Loss	Spear. corr. val.
Sorter baseline	45.7
Sorter CNN	46.6
Sorter LSTM	50.4

Toy experiments:

- Binary classification on synthetic data
- Competitive with less complexity



Object recognition: evaluated on the VOC 2007 challenge



Model	mAP
VGG 16	89.3
WILDCAT [1]	95.0
WILDCAT*	93.2
WILDCAT* + SoDeep	94.0

Evaluation

Cross modal retrieval: evaluated on MS-CoCo image/caption pairs

Query: A cat on a sofa



Model	Caption retrieval				Image retrieval			
	R@1	R@5	R@10	Med. r	R@1	R@5	R@10	Med. r
DSVE-Loc[2]	69.8	91.9	96.6	1	55.9	86.9	94.0	1
GXN[3]	68.5	-	97.9	1	56.6	-	94.5	1
SoDeep	71.5	92.8	97.1	1	56.2	87.0	94.3	1

Memorability prediction: memorability score reflects the probability of a video to be remembered



Model	Spear. corr.
Baseline	46.0
Sem-Emb + MSE loss	48.6
Sem-Emb + SoDeep	49.4

References

- [1] T. Durand et al. Wildcat: Weakly supervised learning of deep convnets for image classification, pointwise localization and segmentation. CVPR, 2017.
- [2] M. Engilberge et al. Finding beans in burgers: Deep semantic-visual embedding with localization. CVPR, 2018.
- [3] J. Gu et al. Look, imagine and match: Improving textual-visual cross-modal retrieval with generative models. CVPR, 2018.
- [4] Y. Yue et al. A support vector method for optimizing average precision. ACM SIGIR, 2007.

Code available on Github



<https://github.com/technicolor-research/sodeep>